

*On an Inversion Point for Liquid Carbon Dioxide in Regard to  
the Joule-Thomson Effect.*

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In a paper published recently in the ‘Philosophical Transactions’ “On the Thermal Properties of Carbonic Acid at Low Temperatures,”\* Prof. C. Frewen Jenkin and Mr. D. R. Pye give, amongst other results, those obtained from a series of measurements of the Joule-Thomson effect for liquid CO<sub>2</sub> at various temperatures. These results are tabulated in Table V of their paper. They are of particular interest because, within the range of temperatures to which they correspond, they find an inversion point for the Joule-Thomson effect, *i.e.*, a temperature at which the effect changes over from being a cooling (at higher temperatures) to being a heating. As they themselves say: “No experiments on the Joule-Thomson effect for liquid CO<sub>2</sub> appear to have been published” previously; and as they admit that it is not easy to say what effect the presence of a trace of air (which was there) may have on their results, any method of testing them should prove of value. Such a test can be made by utilising the values of the specific volumes of liquid CO<sub>2</sub> which they give in a diagram on p. 78 of their paper.

*Method of Test.*

If the drop of pressure employed may be treated as a differential the Joule-Thomson effect is given by the equation

$$C_p \left( \frac{\partial T}{\partial p} \right)_{E+p^v} = T \left( \frac{\partial v}{\partial T} \right)_p - v = T^2 \frac{\partial}{\partial T} \cdot \left( \frac{v}{T} \right)_p.$$

The inversion point must therefore correspond to a minimum (or maximum) value of  $v/T$ .

*Application of Test.*

I have read off from the diagram of specific volumes the values at various pressures and temperatures and calculated the ratios  $v/T$ . These are tabulated below :—

\* ‘Phil. Trans.’ 1913, A, No. 499.

$p = 400 \text{ lb./sq. in.}$ 

$t.$	T.	$v.$	$\frac{v}{T} \times 10^5.$
° C.	Abs.		
-16.5	256.5	0.974	380
-27	246	0.933	379.3
-36	237	0.900	379.7

 $p = 500 \text{ lb./sq. in.}$ 

$t.$	T.	$v.$	$\frac{v}{T} \times 10^5.$
° C.	Abs.		
-4.6	268.4	1.042	380
-16.5	256.5	0.970	378.2
-27	246	0.929	377.6
-36	237	0.897	378.5

 $p = 600 \text{ lb./sq. in.}$ 

$t.$	T.	$v.$	$\frac{v}{T} \times 10^5.$
° C.	Abs.		
+5.7	278.7	1.119	401.5
-4.6	268.4	1.031	384.1
-16.5	256.5	0.967	377.1
-27	246	0.926	376.4
-36	237	0.895	377.6

All these three sets concur in giving a minimum value of  $v/T$  at a temperature not much removed from  $-24^\circ \text{C}$ . The inversion point actually found experimentally lies between  $-20.7^\circ$  and  $-31^\circ$ , and by plotting their cooling effects one finds it to be at  $-28^\circ \text{C}$ , the high pressure being between 668 and 664 lbs./sq. in., and the low pressure between 433 and 360. The mean pressure is therefore about 500 lb./sq. in. Thus, the rather remarkable result that an inversion point exists near the point found is confirmed. The result is remarkable, because it implies that liquid  $\text{CO}_2$  is in this region behaving very nearly like a perfect gas, its volume being nearly proportional to the absolute temperature.

It may be added that 500 lb./sq. in. is about 0.46 times the critical pressure, and  $-28^\circ \text{C}$ . is about 0.81 times the critical temperature; and that these are approximately co-ordinates of an inversion point for any van der Waals liquid.

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